

\* Equivalence of DFA & NFA

There is a DFA  $D$  for any NFA  $N$  i.e.,  
 $L(D) = L(N)$ .

Two finite acceptors,  $M_1$  &  $M_2$  are said to be equivalent if that is, they both accept the same language.

$$L(D) = L(N) \quad \checkmark \text{ equal.}$$

Construction:

→ In DFA or NFA, whenever an arrow is followed, there is a set of possible states. (Set of states is subset of  $Q$ ).

→ Track the information about subsets of states that can be reached from initial state after following arrows.

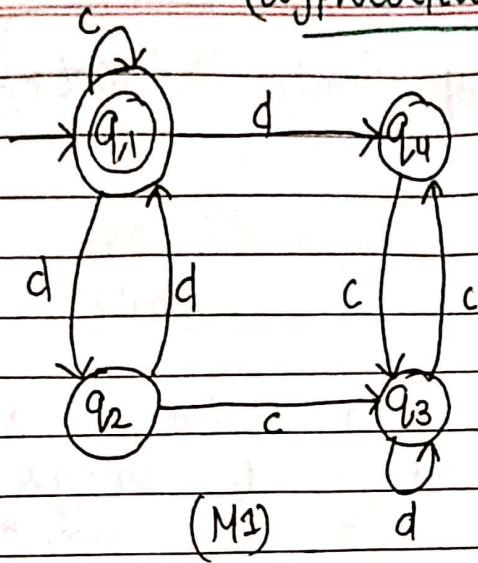
→ Consider each subset of states of NFA as a state of DFA and every subset of states containing a final state as a final state of DFA.

Example / find out the equivalent DFA for the given NFA.

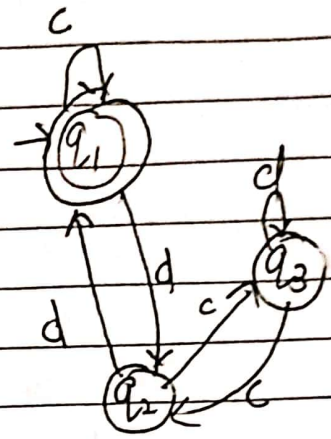
@jnotes

@JPwebdevelopers

Q:



(M1)



(M2)

Transition Table of NFA

Transition Table (DFA)

States	c	d
→ q <sub>1</sub>	q <sub>1</sub>	{q <sub>2</sub> , q <sub>4</sub> }
q <sub>2</sub>	q <sub>3</sub>	q <sub>1</sub>
q <sub>3</sub>	q <sub>4</sub>	q <sub>3</sub>
q <sub>4</sub>	q <sub>3</sub>	∅

States	c	d
→ q <sub>1</sub>	q <sub>1</sub>	q <sub>2</sub>
q <sub>2</sub>	q <sub>3</sub>	q <sub>1</sub>
q <sub>3</sub>	q <sub>2</sub>	q <sub>1</sub>

- Same set of input strings
- Same Initial state
- Same final state

Yes they are equivalent DFA of NFA

Common Table

States	c	d
{q <sub>1</sub> , q <sub>1</sub> }	{q <sub>1</sub> , q <sub>1</sub> }	{q <sub>2</sub> , q <sub>4</sub> , q <sub>2</sub> }
{q <sub>2</sub> , q <sub>2</sub> }	{q <sub>3</sub> , q <sub>3</sub> }	{q <sub>1</sub> , q <sub>1</sub> }
{q <sub>3</sub> , q <sub>3</sub> }	{q <sub>4</sub> , q <sub>2</sub> }	{q <sub>3</sub> , q <sub>3</sub> }
{q <sub>4</sub> }	q <sub>3</sub>	∅

{q<sub>1</sub>, q<sub>1</sub>} → Both final state  
 {q<sub>2</sub>, q<sub>4</sub>, q<sub>2</sub>} → all intermediate states

FS IS    IS FS  
 X            X            ✓